With iodine and chlorine in their standard states of solid and gas, the free energies of formation of the various forms of iodine monochloride as determined by physical chemical methods are as follows: $\mathrm{ICl}(\mathrm{g}), 977$ cal.; $\mathrm{ICl}(\mathrm{l}),-867 \mathrm{cal} . ; \mathrm{ICl}(\mathrm{s}),-887 \mathrm{cal}$.

The degree of dissociation of iodine monochloride gas into gaseous iodine and chlorine has the value $0.42 \%$ at $25^{\circ}$ and $1.58 \%$ at $100^{\circ}$.

The entropy of $\mathrm{ICl}(\mathrm{g})$ at $25^{\circ}$ and one atmosphere is $59.6 \mathrm{cal} . / \mathrm{deg}$. ( 59.2 cal./deg. spectroscopical).

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[Contribution from the Chemical Laboratory of Harvard University]

## THE CRYSTAL STRUCTURE OF RHOMBIC AMMONIUM NITRATE

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No x-ray measurements on the rhombic form (IV) of ammonium nitrate have been published other than the three axial lengths. In addition to rounding out the univalent nitrate group, a complete structure is desirable for the interpretation of some of the unusual properties of this compound, such as birefringence, polymorphism and plastic deformation.

Crystallographic.-According to Groth the crystals are of the rhombic bipyramidal class, axial ratios $0.9092: 1: 1.0553$, density 1.725 , optic axial plane (100), acute bisectrix $b$. Bowen ${ }^{1}$ found $2 \mathrm{~V}=35^{\circ}$ and the refractive indices: electric vector parallel to $b, \alpha=1.41$; parallel to $a, \beta=1.61$; parallel to $c, \gamma=1.64$. This form is stable only in the interval -16 to $+32^{\circ}$.

Methods.-Recrystallization from water at room temperature gave suitable (110) prisms. Molybdenum radiation was employed exclusively; it was filtered in taking powder photographs and a set of $30^{\circ}$ oscillation diagrams about the three axes. In a set of Laue patterns with the primary beam nearly parallel to the three axes, the minimum wave length was 0.30 $\AA$. Intensitites of reflections were estimated visually. All Miller indices refer to the above axes.

Lattice Constants.-The constants determined from zero lines of accurate rotation photographs are: $a=4.92_{8}, b=5.43_{4}, c=5.73_{2}$, ratios $0.9069: 1: 1.0548, Z=2, \mathrm{~V}=76.7$, density $=1.720$. The former are identical with Bragg's values to three figures. ${ }^{2}$

Choice of Structure.-The only systematic extinctions noted were for ( $0 k l$ ) when $k+l$ is odd; assuming holohedral symmetry this indicates $\mathrm{V}_{\mathrm{h}}^{13}$. In disposing the atoms in this space-group primary consideration was

[^0]given to intensity data. It is probable that the nitrate group is a triangle of side $2.10 \AA$. with the distance between oxygen atoms in different groups greater than $3.2 \AA .^{3}$ It has been shown that some nitrates owe their strong double refraction to the arrangement of the nitrate groups in parallel planes, the ray with the electric vector parallel to these planes being the slower, that with the vector perpendicular to them the faster; also the molecular birefringence, $R \omega-R \epsilon$, tends to be constant as the metal ion is changed. ${ }^{4}$ Bragg's extended table proves that ammonium nitrate follows this rule; it is thus to be expected that in it the nitrate planes lie perpendicular to $b$.

|  | $\mathrm{M} / \rho$ | $\omega$ | $\epsilon$ | $\mathrm{R} \omega$ | $\mathrm{R} \mathrm{\epsilon}$ | $\mathrm{R} \omega$-R $\epsilon$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{LiNO}_{3}$ | 28.9 | 1.735 | 1.435 | 11.60 | 7.54 | 4.06 |
| $\mathrm{NaNO}_{3}$ | 37.45 | 1.587 | 1.336 | 12.58 | 7.75 | 4.83 |
| $\mathrm{KNO}_{3}$ | 47.85 | 1.506 | 1.335 | 14.36 | 9.90 | 4.46 |
| $\mathrm{NH}_{4} \mathrm{NO}_{3}$ | 46.35 | 1.625 | 1.41 | 16.38 | 11.48 | 4.90 |

There are two orientations of the crystal axes $a b c$ in the structure axes XYZ that give the extinctions noted, (A) $a b c$ in $Z Y X$ and (B) $a b c$ in YZX. There are two arrangements which give nitrate groups of the desired configuration; taking point designations from Wyckoff and indicating ammonium and nitrate nitrogens by Nh and No , respectively, these are (I) Nh in (a), No and O in (b), O in (e) and (II) Nh in (b), No and O in (a), O in (f). Of the four arrangements IA and IIB have the same structure factor, which is constant for sets of reflections where only $l$ varies by 2 ; they are excluded by the following sets: 101 absent, 103 vs; 201 vw , 203 vs; 111 vs, 113 w . Similarly in IB and IIA sets where only $k$ varies by 2 have the same structure factor; the observed intensities consistently follow this relation through Table I. IB alone has the too low oxygenoxygen distance $2.84 \AA$., depending only on $a$ and the side of the nitrate triangle; also IIA is more consistent with the abnormal intensity decline of reflections ( $h 00$ ) than IB. Finally IIA alone has the nitrate planes perpendicular to $b$. It was selected and the coördinates rewritten.

| Position, $\mathrm{V}_{\mathrm{h}}^{\text {a }}$ | $k+l$ even | $k+l$ odd |
| :---: | :---: | :---: |
| $\mathrm{Nh}(\mathrm{b}) z^{1 / 2} \mathbf{0}, \mathrm{z} \mathrm{O}^{1 / 2}$ | $\begin{aligned} & \pm 2 \mathrm{~F} \cos h 2 \pi z \\ & \quad \text { (plus for } l \text { even) } \end{aligned}$ | $\begin{aligned} & \pm 2 \mathrm{~F} \sin h 2 \pi z \\ & \quad \text { (plus for } l \text { odd) } \end{aligned}$ |
| No (a) $x 00, \bar{x}^{1 / 2}{ }^{1 / 2}$ | $2 \mathrm{~F} \cos h 2 \pi x$ | $2 \mathrm{~F} \sin h 2 \pi x$ |
| O (a) $\mathrm{y} 00, \bar{y}^{1 / 2}{ }^{1 / 2}$ | 2F $\cos h 2 \pi y$ | $2 \mathrm{~F} \sin h 2 \pi y$ |
| $\begin{gathered} \mathrm{O} \text { (f) } v 0 u, \overline{\bar{v}}^{1 / 2} / 2+u \\ v 0 \bar{u}, \bar{v}^{1 / 2} / 2^{1 / 2}-u \end{gathered}$ | $4 \mathrm{~F} \cos 22 \pi u, \cos h 2 \pi v$ | $4 \mathrm{~F} \cos l 2 \pi u, \sin h 2 \pi v$ |

Choice of Parameters.-In calculating structure factors $F$ curves for ammonium, ${ }^{5}$ nitrogen and oxygen ${ }^{6}$ were used. Since the structure factor
${ }^{3}$ D. A. Edwards, Z. Krist., 80, 154 (1931).
${ }^{4}$ W. L. Bragg, Proc. Roy. Soc. (London), A105, 370 (1924); A106, 346 (1924).
${ }^{5}$ R. W. G. Wyckoff, "The Structure of Crystals," 1931.
' R. W. James and G. W. Brindley, Z. Krist., 78, 470 (1931).
for reflections ( 0 kl ) depends only on $u$, their observed intensities offer a check on this parameter, $2 c u$ being one side of the nitrate triangle; the value cited showed satisfactory agreement and was retained. It makes the shortest oxygen-oxygen distance independent of $x 3.26 \AA$. Assuming the nitrate triangles are equilateral, only $x$ and $z$ now remain independently


Fig. 1.-Unit cell of ammonium nitrate projected on (001) and (010). The height of each atom is indicated in Ångström units.
variable. The value of $x$ was estimated from the intensities of Laue reflections at large $\sin \vartheta / \lambda$ where $F_{\mathrm{Nh}}$ is one-third or less of $F_{\mathrm{O}}$ or $F_{\mathrm{No}}$, and $z$ follows from the intensities of powder and oscillation reflections. The structure factors ( $F^{2}$ ) of Table I are calculated for the tabulated values

| Parameters |  |  |  | Distances |
| :--- | ---: | :--- | :--- | :--- |
| $u$ | $66^{\circ}$ | 0.183 | $1.05 \AA$. | Nh - No: $3.36,3.48$ |
| $x$ | 180 | .500 | 2.47 | O-O: $3.08,3.26,3.33$ |
| $y$ | -90 | .750 | 3.70 | Each Nh: 2.96 (two oxygen atoms), 2.96 (two atoms) |
| $v$ | 135 | .375 | 1.85 |  |
| $z$ | 35 | .097 | 0.48 | 3.18 (two atoms), 3.21 (two atoms) |
| z (four atoms), average of $12=3.13$ |  |  |  |  |

of the parameters; the disagreements with observed intensities are unsystematic and are not considered prohibitive. The calculated distances are similar to those prevailing in like substances except that the first oxygen-oxygen distance is about $3 \%$ below the minimum observed and predicted by Zachariasen. ${ }^{7}$
${ }^{7}$ W. H. Zachariasen, Z. Krist., 80, 137 (1931).

Table I
Observed Intensities of Reflections from Ammonium Nitrate

|  | $\frac{\sin \vartheta}{\lambda}$ | $F^{2}$ | Intensity |  | ${ }_{h k l} \frac{\sin \vartheta}{\lambda}$ |  | $F^{2}$ | Intensity |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $n k l$ |  |  | Osc. | Laue |  |  | Osc. | Laue |
| 020 | 0.184 | 665 | vs | vs* | 033 | 0.380 |  | 0 | 0 |  |
| 040 | . 368 | 166 | S |  | 053 | . 530 | 0.2 | 0 |  |
| 060 | . 552 | 66 | m |  | 004 | . 350 | 41 | S |  |
| 011 | . 127 | 58 | vs | s* | 024 | . 394 | 32 | S |  |
| 031 | . 290 | 36 | 5 | $\mathrm{m}^{*}$ | 044 | . 507 | 18 | m |  |
| 051 | . 468 | 22 | m | m | 015 | . 445 | 45 | s | m |
| 002 | . 175 | 54 | vs | m* | 035 | . 516 | 37 | m |  |
| 022 | . 254 | 22 | s | $\mathrm{m}^{*}$ | 006 | . 524 | 71 | m |  |
| 042 | . 407 | 8.3 | m |  | 026 | . 554 | 61 | m |  |
| 013 | . 277 | 30 | m |  | 017 | . 616 | 7.5 |  | 0 |
| 100 | . 101 | 47 | vs | s* | 110 | . 137 | 2.6 | S | O* |
| 120 | . 210 | 27 | vs | $\mathrm{m}^{*}$ | 130 | . 294 | 0 | W | $\mathrm{O}^{*}$ |
| 140 | . 382 | 19 | m |  | 101 | . 134 | 2.4 | 0 | O* |
| 111 | . 162 | 139 | vs | vs* | 121 | . 228 | 0.4 | 0 | O* |
| 131 | . 307 | 42 | S | vs | 141 | . 392 | 0 | 0 | 0 |
| 151 | . 479 | 17 | m | $s$ | 112 | . 222 | 162 | vs |  |
| 102 | . 202 | 61 | vs |  | 132 | . 342 | 60 | S |  |
| 122 | . 273 | 25 | s |  | 152 | . 502 | 22 | m | S |
| 142 | . 419 | 3.6 | w | m | 172 | . 674 | 11 |  | w |
| 162 | . 587 | 0.3 |  | 0 | 103 | . 279 | 60 | vs | $\mathrm{m}^{*}$ |
| 113 | . 294 | 0.6 | w | O* | 123 | . 334 | 43 | S | $\mathrm{m}^{*}$ |
| 133 | . 392 | 0.1 | vw | m | 143 | . 462 | 22 | m | s |
| 153 | . 539 | 0 | 0 | w | 114 | . 375 | 21 | s | S |
| 104 | . 363 | 0.2 | 0 | 0 | 134 | . 456 | 12 | m | S |
| 124 | . 407 | 0 | 0 | w | 154 | . 586 | 6.6 |  | m |
| 144 | . 517 | 0.4 | 0 | w | 105 | . 448 | 2 | 0 | 0 |
| 115 | . 457 | 35 | $s$ | $s$ | 125 | . 484 | 1.5 | 0 | 0 |
| 135 | . 526 | 25 | m | s | 145 | . 580 | 0.6 |  | 0 |
| 155 | . 641 | 17 |  | w | 210 | . 222 | 220 | vs |  |
| 200 | . 203 | 2.3 | m |  | 230 | . 342 | 75 | S |  |
| 220 | . 274 | 1.0 | w |  | 250 | . 502 | 28 | w |  |
| 240 | . 420 | 0 | vw |  | 270 | . 674 | 11 |  | w |
| 211 | . 239 | 18 | s | w* | 201 | . 221 | 0.2 | vw | O* |
| 231 | . 353 | 4 | w |  | 221 | . 288 | 0 | 0 | $\mathrm{O}^{*}$ |
| 251 | . 509 | 0.4 | 0 | 0 | 241 | . 429 | 0.3 | 0 | 0 |
| 202 | . 268 | 1.3 | 0 | O* | 212 | . 283 | 5.2 | m | O* |
| 222 | . 324 | 0.5 | 0 |  | 232 | . 384 | 4 | w |  |
| 242 | . 455 | 0 | 0 |  | 252 | . 531 | 3.2 | 0 | 0 |
| 213 | . 344 | 28 | m | s | 203 | . 331 | 82 | vs |  |
| 233 | . 431 | 1.4 | w |  | 223 | . 379 | 55 | S |  |
| 253 | . 566 | 0.2 |  | 0 | 243 | . 495 | 27 | m |  |
| 204 | . 404 | 0 | w |  | 263 | . 644 | 13 |  | m |
| 224 | . 444 | 0 | w |  | 214 | . 414 | 1.2 | w | w |
| 244 | . 546 | 0 | 0 |  | 234 | . 489 | 0.5 | W |  |
| 215 | . 490 | 0.6 | 0 | 0 | 205 | . 481 | 7 | vw |  |
| 235 | . 554 | 0.2 |  | 0 | 225 | . 515 | 6.8 |  | w |
| 300 | . 304 | 6.9 | 0 |  | 310 | . 318 | 36 | s |  |

Table I (Concluded)

|  | $\underline{\sin \vartheta}$ |  | Intensity |  | $\underline{\sin v}$ |  |  | Intensity |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| hkl | $\lambda$ | $F^{2}$ | Osc. | Laue | $h k l$ | $\lambda$ | $F^{2}$ | Osc. | Laue |
| 320 | 0.356 | 3.6 | O |  | 330 | 0.411 | 21 | m |  |
| 340 | . 477 | 0.9 | 0 |  | 301 | . 317 | 70 | S | $s$ |
| 311 | . 330 | 0.6 | m | m | 321 | . 366 | 45 | S | vs |
| 331 | . 420 | 0 | w | m | 312 | . 363 | 4.3 | m | s |
| 302 | . 350 | 30 | S |  | 332 | . 446 | 1.6 | w | m |
| 322 | . 396 | 25 | s |  | 303 | . 401 | 0.7 | vw |  |
| 313 | . 412 | 25 | S | S | 323 | . 442 | 0.4 | w |  |
| 333 | . 487 | 19 | m |  | 314 | . 471 | 0.5 | 0 | w |
| 304 | . 463 | 6.5 | m |  | 334 | . 539 | 0.7 | 0 |  |
| 324 | . 498 | 6 | m | S | 410 | . 416 | 1.3 | vw | m |
| 400 | . 406 | 4.5 | 0 |  | 430 | . 491 | 0.6 | O |  |
| 420 | . 445 | 2.8 | 0 |  | 401 | . 414 | 1.3 | m | s |
| 411 | . 424 | 13 | m | S | 421 | . 454 | 0.8 | m | m |
| 431 | . 498 | 9 | m | m | 412 | . 451 | 0.8 | 0 | w |
| 402 | . 441 | 40 | S |  | 432 | . 521 | 0.5 |  | 0 |
| 422 | . 478 | 36 | m |  | 403 | . 483 | 0.6 | m |  |
| 413 | . 491 | 81 | S | s | 423 | . 516 | 0.5 | w | m |
| 433 | . 556 | 61 |  | S | 510 | . 515 | 26 | m | S |
| 500 | . 507 | 0 | 0 |  | 530 | . 577 | 11 | m |  |
| 520 | . 539 | 0 |  | 0 | 501 | . 515 | 10 | m | s |
| 511 | . 523 | 0.2 | w | w | 521 | . 546 | 9 | w | m |
| 531 | . 584 | 0 |  | 0 | 512 | . 544 | 0 | w | m |
| 502 | . 536 | 21 | m | m | 532 | . 603 | 0 |  | W |
| 522 | . 567 | 18 | w | m | 503 | . 570 | 0.5 | 0 | 0 |
| 513 | . 578 | 13 | W | W | 523 | . 600 | 0.4 |  | 0 |

* Powder reflection.

Discussion.-A marked feature of the structures of lithium, sodium and potassium nitrates is the separation into alternate layers of metal ions and nitrate groups which lie parallel to the nitrate planes. In the present form of the ammonium compound this characteristic is absent, although there is a suggestion of such layering in the direction of the $a$-axis perpendicular to the nitrate planes. This structure may be considered as related to the cesium chloride type if the nitrate groups are taken as units.

I am grateful to Professor Albert Sauveur for the use of x-ray apparatus.

## Summary

A complete structure is proposed for rhombic ammonium nitrate in the space group $V_{h}^{13}$. As in some other univalent nitrates, the strong double refraction is probably to be explained by the arrangement of the nitrate groups in parallel planes.

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[^0]:    ${ }^{1}$ N. L. Bowen, J. Phys. Chem., 30, 722 (1926).
    ${ }^{2}$ W. H. Bragg, Trans. Faraday Soc., 20, 59 (1924).

